

P 1/73. If  $x$  and  $y$  are positive and unequal, prove that

$$(i) \quad \frac{x}{2y+x} + \frac{y}{2x+y} > \frac{2}{3}$$

$$(ii) \quad \frac{x}{y+2x} + \frac{y}{x+2y} < \frac{2}{3}$$

(P.H.Diananda)

P 2/73. Find the largest number that can be obtained as a product of two positive integers whose sum is a given positive integer  $s$ . (L.Y.H.Yap)

P 3/73. Let  $m_1, m_2, \dots$  be a sequence of positive integers.

Must  $\frac{m_1^2 + \dots + m_n^2}{(m_1 + \dots + m_n)^2}$  necessarily converge to zero as

$n$  tends to infinity? If not, what is a necessary and sufficient condition for it to converge to zero? Can this problem be generalised? (L.H.Y. Chen)

P 4/73. Prove 
$$\int_0^x \frac{t^n}{1+t} dt = \int_0^x \frac{(x-t)^n}{(1+t)^{n+1}} dt$$

(K.M. Chan)

P 5/73. Let  $p(x) = a_0 + a_1x + \dots + a_nx^n$  be a polynomial with integral coefficients, and let  $x_1$  be an even integer and  $x_2$  an odd integer. If  $p(x_1)$  and  $p(x_2)$  are both odd, prove that  $p(x) = 0$  has no integral roots.

[Hint: Try, for example  $x_1 = 0, x_2 = 1$ .] (T.A.Peng)

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#### ACKNOWLEDGEMENTS

The Society wishes to thank

1. Federal Publications Sdn. Bhd. for their books:  
*Contemporary School Mathematics*, vols. 1 - 4; and  
*Mathematical Structures* by H.T. Combe;

2. The authors Hector Chee and Lian Sek Lin for their books *New Mathematics for Secondary Schools*, vols. 1 - 4;
3. Dr. Tony Tan for the following journals:
  - (i) *Operations Research*, 1965 - 1973.
  - (ii) *Directory of Operations Research Society of America*, 1966 - 1972.
  - (iii) *International Abstracts in Operations Research*, 1965 - 1971.
  - (iv) *Bulletin of the Operations Research Society of America*, 1965 - 1969.
  - (v) *Transportation Science*, 1967 - 1971.
  - (vi) *Management Science*, 1967 - 1972.

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In our next issue, we shall start a book section where summary book reviews would be given. These reviews would include comments which would be useful to students and teachers of mathematics. Publishers and authors of mathematical books of any level are invited to send them to the Editors, Mathematical Medley, c/o Department of Mathematics, University of Singapore.