

Once every four years, mathematicians from various parts of the world gather under the auspices of the International Mathematical Union (IMU) to talk about their research work, communicate with each other and witness the presentation of the prestigious Fields medal.

The awarding of the Fields medal was initiated in 1936 at Oslo and, except for a hiatus of fourteen years covering the Second World War, has generated since then much interest and expectations within the mathematical community. The Fields medal is popularly regarded as the equivalent of the Nobel prize in mathematics. A notable difference is that the former is traditionally awarded to mathematicians below the age of forty with the objective that "while it was in recognition of work already done it was at the same time intended to be an encouragement for further achievement on the part of the recipients and a stimulus to renewed effort on the part of others" - in the words of John Charles Fields (1863 - 1932), a mathematician and Chairman of the Committee of the 1924 International Mathematical Congress, who bequeathed part of his estate to the setting up of a trust for the award. On the material side, each recipient of the award receives a gold medal and a sum of 1500 Canadian dollars.

The complete list of Fields medallists is given below. The areas in which the award-winning contributions were made are also indicated.

1936, Oslo Lars Valerian Ahlfors (b. 1907),  
Harvard University; Complex analysis

Jesse Douglas (b. 1897), Massachusetts  
Institute of Technology; Minimal  
surfaces

- 1950, Cambridge  
(Massachusetts) Laurent Schwartz (b. 1915), University  
of Nancy, Analysis  
Alte Selberg (b. 1917), Institute  
for Advanced Study, Princeton; Number  
theory
- 1954, Amsterdam Kunihiro Kodaira (b. 1915), Princeton  
University; Differential topology  
Jean-Pierre Serre (b. 1926), Univer-  
sity of Paris; Number theory, topology
- 1958, Edinburgh Klaus Friedrich Roth (b. 1925),  
University of London; Number theory  
René Thom (b. 1923), University of  
Strasbourg; Differential topology
- 1962, Stockholm Lars V. Hörmander, University of  
Stockholm; Several complex variables  
John Willard Milnor (b. 1931), Prince-  
ton University; Differential topology
- 1966, Moscow Michael Francis Atiyah (b. 1929),  
Oxford University; Topology  
Paul Joseph Cohen (b. 1934), Stanford  
University; Set theory  
Alexandre Grothendieck, University of  
Paris; Algebraic geometry  
Stephen Smale (b. 1930), University of  
California, Berkeley; Global analysis
- 1970, Nice Alan Baker, Cambridge University;  
Number theory  
Heisuke Hironaka, Harvard University;  
Algebraic geometry  
Sergei P. Novikov (b. 1938), Moscow

University; Topology

John G. Thompson, Cambridge University;

Group theory

1974, Vancouver

Enrico Bombieri, University of Pisa;

Number theory, Minimal surfaces

David B. Mumford (b. 1937), Harvard  
University; Algebraic geometry

This year the Congress will be held at Helsinki, Finland, from 15 August to 23 August. In addition to the presentation of the Fields medals at the opening ceremony, the mathematical activities will include seventeen one-hour plenary addresses in the form of broad surveys of recent progress in various fields of mathematics, more than one hundred 45-minute addresses in specified sections and numerous 10-minute oral communications by participants. A new feature of this Congress is the introduction of 1½-hour poster sessions whereby participants may display their work on given bulletin boards. During the Congress, a symposium on the Mathematical Training of Mathematics Teachers will be organized by the International Commission on Mathematical Institution.

The one-hour plenary addresses and the 45-minute addresses are given below.

*One-hour plenary addresses*

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|----------------|--|
| L. V. Ahlfors  | Quasiconformal mappings, Teichmüller spaces, and Kleinian groups     |
| A. P. Calderon | Commutators, singular integrals on Lipschitz curves and applications |
| A. Connes      | On the classification of von Neumann algebras                        |
| R. Dobrushin   | Classical statistical mechanics as a                                 |

- branch of probability theory
- D. Edwards The topology of manifolds and cell-like maps
- Gorenstein The classification of finite simple groups
- Kashiwara Micro-local analysis
- N. Krasovskii Control under uncertain information and differential games
- Langlands Automorphic representations and L-functions
- Manin Modular forms and number theory
- Novikov Linear operators and integrable Hamiltonian system
- Penrose The complex geometry of the natural world
- Schmid Representations of semisimple Lie groups
- N. Shiriyayev On absolute continuity and singularity of probability measures on functional spaces
- P. Thurston Geometry and topology in dimension three
- Weil History of mathematics : why and how
- T. Yau The role of partial differential equations in differential geometry

*45 - minute addresses in sections*

1. Mathematical logic and foundations of mathematics
- H. Conway Arithmetical operations on transfinite numbers

- L. Harrington Definability theory
- A. Macintyre Nonstandard number theory
- G. S. Makanin Rešenie problemy razrešimosti  
uravnenií svobodnoí polugruppe
- D. A. Martin Infinite games
2. Algebra
- M. Aschbacher A survey of the classification  
program for finite simple groups of  
even characteristic
- K. S. Brown Cohomology of groups
- B. Fischer Sporadische endliche einfache Gruppen
- M. Hochster Cohen-Macaulay rings and modules
- V. Kac Lie superalgebras
- W. van der Kallen Generators and relations in algebraic  
K-theory
- V. P. Platonov Algebraic groups and reduced K-theory
- A. V. Roiter Matrix problems
- A. Suslin The cancellation problem for projective  
modules and some related topics
3. Number theory
- G. Choodnovsky Algebraic independence of values  
of exponential and elliptic functions
- J. H. Coates The arithmetic of elliptic curves with  
complex multiplication
- H. Iwaniec Sieve methods
- N. M. Katz P-adic L-functions
- G. Shimura On some problems of algebraicity
- R. Tijdeman Upper bounds for solutions of

exponential diophantine equations

C. Vaughan Recent work in additive prime number theory

#### 4. Geometry

Bogoyavlensky On manifolds, satisfying Einstein equations with hydrodynamical stress-energy tensor

Connelly Conjectures and open questions in rigidity

do Carmo Minimal surfaces

Gromov Synthetic geometry

M. Harlamov Real algebraic surfaces

G. Larman Recent advances in convexity

Osserman Isoperimetric inequalities and eigenvalues of the laplacian

Shiohama Convex sets and convex functions on complete manifolds

#### 5. Topology

W. Cannon The recognition problem : what is a topological manifold? A solution to the double suspension problem for homology spheres.

E. Cappell Singularities of immersions and embeddings

J. Casson Knot cobordism

Fuks New results on the characteristic classes of foliations

Hatcher Linearization in 3-dimensional topology

- J. Lin The topology of finite H-spaces
- I. Madsen Spherical space forms
- S. Mardešić Shape theory
- D. C. Ravenel Complex cobordism and its applications  
to homotopy theory
- J. E. West Hilbert cube manifold - meeting  
ground of geometric topology and  
absolute neighborhood retracts

## 6. Algebraic geometry

- S. Bloch K-theory and zeta functions of  
elliptic curves
- F. A. Bogomolov Unstable vector bundles and families  
of curves on surfaces
- D. Gieseker Some applications of geometric in-  
variant theory to moduli problems
- E. Looijenga Homogeneous spaces associated to  
certain semiuniversal deformations
- C. Procesi Standard monomials, Young diagrams  
and invariant theory
- S. Ramanan Vector bundles on algebraic curves
- K. Ueno Classification of algebraic manifolds

## 7. Lie groups, algebraic groups, automorphic functions

- I. Bernstein Induced representations of  $GL(n)$   
over p-adic field
- W. Casselman Jacquet modules for real groups
- V. G. Drinfeld Langlands' conjecture for  $GL(2)$  over  
functional fields
- G. R. Kempf Algebraic representations of reductive  
groups

- Lepowsky Lie algebras and combinatorics
- Piatetski-Shapiro Tate theory for reductive group
- Shintani On special values of zeta functions  
of totally real algebraic number  
fields

8. Real and functional analysis

- Beckner Basic problems in Fourier analysis
- V. Boskarov Method of averaging in the theory of  
orthogonal series
- Foias Contractive intertwining dilations and  
waves in layered media
- M. Garsia Some combinatorial methods in real  
analysis
- M. Nikishin The Pade approximants
- K. Nikol'skii What problems the spectral theory and  
complex analysis can solve one for  
another?

9. Complex analysis

- Baernstein How the \*-function solves extremal  
problems
- A. Griffiths Holomorphic mappings in one and  
several complex variables
- Korenblum Analytic functions of unbounded  
characteristic and Beurling algebra
- Moser The holomorphic equivalence problem  
for real hypersurfaces
- T. Siu Extension problems in several complex  
variables

- H. Skoda Integral methods and zeros of holomorphic functions
- J. Väisälä Survey on quasiregular maps in  $\mathbb{R}^n$
10. Operator algebras and group representations
- J. Dixmier Enveloping algebras
- R. G. Douglas Extensions of  $C^*$ -algebras and algebraic topology
- A. Kirilov Infinite dimensional groups; their orbits and representations
- S. Sakai Recent developments in the theory of unbounded derivations in  $C^*$ -algebras
- J. R. Wallach The spectrum of compact quotients of semi-simple Lie groups
- G. J. Zuckerman Coherent translation of characters of semi-simple Lie groups
11. Probability and mathematical statistics
- A. Borokov Rate of convergence and large deviations for invariance principle
- C. Dellacherie A survey of the theory of stochastic integrals
- M. Fukushima Dirichlet spaces and additive functionals of finite energies
- P. Revesz Some properties of the coin-tossing sequence
- S. R. S. Varadhan Some problems of large deviations
- A. D. Wentzell Large deviations for stochastic processes

## 12. Partial differential equations

- J. Almgren, Jr. Minimal surfaces : tangent cones, singularities, and topological types
- A. Ivrii Propagation of singularities of solutions of symmetric hyperbolic systems
- E. McKean Riemann surfaces of infinite genus arising from nonlinear wave equations
- B. Melrose The singularities of solutions to boundary value problems
- H. Rabinowitz Critical points of indefinite functionals and periodic solutions of differential equations
- J. Sjostrand Eigenvalues for some hypoelliptic operators and related constructions
- A. Weinstein Eigenvalues of the laplacian plus a potential

## 13. Ordinary differential equations and dynamical systems

- D. Bruno Formal and analytical integral sets
- R. Herman Recent results on differentiable conjugacy of diffeomorphisms
- I. Ilyashenko Global and local aspects of geometric theory of complex differential equations
- J. Mallet-Paret Generic theory for functional differential equations
- R. McGehee Singularities in classical celestial mechanics
- J. Palis, Jr. Bifurcations and moduli of stability

## 14. Control theory and optimization problems

- P. Brunovsky On the structure of optimal feedback

- H. Skoda systems
- F. H. Clarke Nonsmooth analysis and optimization
- L. Ekeland Non-convex variational problems
- N. V. Krylov The control of the diffusion type processes
- H. J. Sussman Analytic stratifications and control theory

#### 15. Mathematical physics and mechanics

- H. Araki Some topics in quantum statistical mechanics
- M. F. Atiyah Geometrical aspects of Gauge theories
- J. L. Bona Model equations for waves in nonlinear dispersive systems
- L. D. Faddeev Quantum theory solitons
- J. Frohlich The mathematics of phase transitions and critical phenomena
- A. M. Jaffe Introduction to Gauge theories
- Ya. G. Sinai Scaling in the theory of phase transitions

#### 16. Numerical analysis

- C. de Boor Splines and B-splines
- J. Nitsche Finite element approximations to the one-dimensional Stefan problems
- P. A. Raviart Finite elements and duality
- A. A. Samarskii 0 cislennom resenii zadac matematicheskoj fiziki
- V. Thomée Galerkin-finite element methods for parabolic equations

Discrete mathematics and mathematical aspects of computer science

W. Haken Combinatorial aspects of some mathematical problems

S. V. Jablonskiĭ On some results in the theory of functional systems

G.-C. Rota Recent progress in combinatorics

G. Rozenberg Some recent developments in formal language theory

C. C. Sims Group theoretic algorithms, a survey

D. Uhlig On the synthesis of self-correcting circuits

18. Mathematics in the social and biological science

R. J. Aumann Recent developments in the theory of the Shapley value

S. I. Rubinow Some contributions to mathematical biology

19. History and education

T. F. Banchoff Computer animation and the geometry of surfaces in 3- and 4-space

A. I. Markushevich Nekotorye voprocы razvitija teorii analitičeskih funkcii v XIX veke

Note The Secretary of the *Society*, Dr Chong Chi Tat, will attend the General Assembly of the IMU on 11-12 August, held in conjunction with the Congress, as the delegate from Singapore with financial support from the IMU fund for travel grant for young mathematicians. He will also participate in the Congress.